SkiLD: Unsupervised Skill Discovery Guided by Local Dependencies

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Abstract

 Unsupervised skill discovery carries the promise that an intelligent agent can learn reusable skills through autonomous, reward-free environment interaction. Existing unsupervised skill discovery methods learn skills by encouraging distinguishable behaviors that cover diverse states. However, in complex environments with many state factors (e.g., household environments with many objects), learning skills that cover all possible states is impossible, and naively encouraging state diversity often leads to simple skills that are not ideal for solving downstream tasks. This work introduces Skill Discovery from Local Dependencies (SkiLD), which leverages state factorization as a natural inductive bias to guide the skill learning process. The key intuition guiding SkiLD is that skills that induce diverse **interactions** between state factors are often more valuable for solving downstream tasks. To this end, SkiLD develops a novel skill learning objective that explicitly encourages the mastering of skills that effectively induce different interactions within an environment. We evaluate SkiLD in several domains with challenging, long-horizon sparse reward tasks including a realistic simulated household robot domain, where SkiLD successfully learns skills with clear semantic meaning and shows superior performance compared to existing unsupervised reinforcement learning methods that only maximize state coverage.

1 Introduction

 Reinforcement learning (RL) achieves impressive successes when solving decision-making problems with well-defined reward functions [\[62,](#page-13-0) [19,](#page-10-0) [31\]](#page-11-0). However, designing this reward function is often not trivial [\[6\]](#page-9-0). In contrast, humans and other intelligent creatures can learn, without external reward supervision, behaviors that produce repeatable and predictable changes in the environment [\[17\]](#page-10-1). These behaviors, which we call *skills*, can be later repurposed to solve downstream tasks efficiently. One of the promises of this form of unsupervised RL is to endow artificial agents with similar capabilities to discover reusable skills without explicit rewards.

 One predominant strategy of prior skill discovery methods focuses on training skills to reach diverse states while being distinguishable [\[18,](#page-10-2) [57,](#page-12-0) [48\]](#page-12-1). However, in complex environments that contain many *state factors*—distinct elements such as individual objects in a household (a formal description in Sec. [2.1\)](#page-1-0), the exponential number of distinct states makes it impossible to learn skills that cover every state. Consequently, these methods result in simple skills that only change the easy-to-control factors (e.g., in a manipulation task moving the agent itself to diverse positions or manipulating each factor independently), and fail to cover other desirable but challenging behaviors. Unsurprisingly, these simple skills often struggle to solve meaningful tasks, resulting in poor downstream performance.

 Our key insight is that, given a factored state space, the interactions between state factors can often act as a powerful inductive bias in guiding the learning of useful skills. For example, in a household

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Figure 1: Skill Discovery from Local Dependencies (SkiLD) describes skills that encode interactions (i.e., local dependencies) between state factors. In contrast to prior diversity-based methods that can easily get stuck by moving the robot to diverse, but non-interactive states, and factor-based methods that are trained to manipulate the hammer and nail, but not their interactions, SkiLD not only manipulate each object (left, middle) but also induce interactions between them (right), by specifying different local dependencies. These skills are often more useful than the "easy" skill learned by previous methods for downstream task-solving.

environment, a skill that induces interactions between a knife and a fruit is more likely to encode

fruit-cutting behaviors that can be crucial for a wide range of downstream kitchen tasks. Furthermore,

 exploring state coverage within the space of interaction states can uncover desirable interactions like cutting the peach.

 The guiding principle behind this inductive bias is that many domains, including robotic manipulation, exhibit dynamic bottlenecks through interactions. Interactions act as dynamic bottlenecks by serving

as particular sets of states that must be reached to control another factor. For example, contact between

the knife and fruit is required to control the fruit through cutting. Instead of simply searching for

diversity alone, which in a large state space could focus only on manipulating single factors, forcing

diversity through interactions prevents these dynamic bottlenecks from blocking a wide coverage of

skills.

 To this end, we introduce Skill Discovery from Local Dependencies (SkiLD), a novel skill discovery method that explicitly learns skills that induce diverse interactions. Specifically, SkiLD models the interactions between state factors using the framework of *local dependencies* (where local refers to state-specific, see details in Sec. [2.2\)](#page-2-0) and proposes a novel intrinsic reward that 1) encourages the agent to induce specified interactions, and 2) encourages the agent to discover diverse ways of inducing specified interaction, as visualized in Figure [2.](#page-3-0) During skill learning, SkiLD gradually discovers new interactions and learns to induce them, based on the skills that it already mastered, resulting in a diverse set of interaction-inducing behaviors that can be readily repurposed for downstream tasks. During task learning, the skill policy is reused, and a task-specific policy is learned to select (a sequence of) skills to maximize task rewards efficiently.

 We evaluate the performance of SkiLD on factor-rich environments with 10 downstream tasks against existing unsupervised reinforcement learning methods. Our experiments indicate that SkiLD learns

to induce diverse interactions and outperforms other methods on most of the examined tasks.

2 Background

 In this paper, our unsupervised skill discovery method is set up in a factored Markov decision process and builds off previous diversity-based methods, as described in Sec. [2.1.](#page-1-0) To enhance the expressivity of skills, our method further augments the skill representation with interactions between state factors,

which we formalize as local dependencies as described in Sec. [2.2.](#page-2-0)

2.1 Factored Markov Decision Process (Factored MDP)

 We consider unsupervised skill discovery in a reward-free Factored Markov Decision Process [\[7\]](#page-9-1) 68 defined by the tuple $\mathcal{M} = (\mathcal{S}, \mathcal{A}, p)$. $\mathcal{S} = \mathcal{S}^1 \times \cdots \times \mathcal{S}^N$ is a factored state space with N subspaces, 69 where each subspace S^i is a multi-dimensional continuous or discrete random variable. Then, zo correspondingly, each state $s \in S$ consists of N state factors, i.e., $s = (s^1, \dots, s^N), s^i \in S^i$. In this paper, we use uppercase letters to denote random variables and lowercase for their specific values (e.g., 72 S denotes the random variable for states s). A is the action space, and p is an unknown Markovian transition model that captures the probability distribution over the next state $S' \sim p(\cdot | S, A)$.

74 The factorization in S inherently exists in many environments, and is a common assumption in prior unsupervised skill discovery works [\[21,](#page-10-3) [27\]](#page-10-4). For example, in robotics, an environment typically τ consists of a robot and several objects to manipulate, and, for each object, S^i would represent its attributes of interest, like pose. In this work, we explore how we can utilize a given state factorization to improve unsupervised skill discovery. In practice, the factorization can either be directly provided by the environment or obtained from image observations with existing disentangled representation learning methods [\[45,](#page-12-2) [29\]](#page-11-1). Following prior work, our method consists of two stages—skill learning and task learning. During the 82 skill learning phase, we seek to learn a skill policy $\pi_{\omega}(\cdot|s, z)$, which defines a conditional distribution 83 over actions given the current state s and some skill representation z , where skills indicate the desired behaviors of the agent. Once the skills are learned, they can be chained together to solve downstream tasks during the task learning phase through an extrinsic reward-optimizing policy. During task

86 learning, a downstream task reward function $r : \mathcal{S} \times \mathcal{A} \to \mathbb{R}$ is provided by the environment. A 87 high-level policy $\pi(z|s)$ is then trained to optimize the expected return through outputting correct

88 skills z given state s .

⁸⁹ 2.2 Identifying Local Dependencies between State Factors

 A key insight of SkiLD is to utilize interactions (or, formally, local dependencies) between state factors as part of the skill representation. In later sections, these local dependencies are compiled 92 into a binary matrix $\mathbb{G}(s, a, s') = \{0, 1\}^{N \times (N+1)}$ representing the local dependencies between all factors. In this section, we first formally define local dependencies, introduce their identification, and finally discuss their application to factored MDPs.

⁹⁵ SkiLD takes a causality-inspired approach for defining and detecting local dependencies [\[5,](#page-9-2) [56\]](#page-12-3), ⁹⁶ where we use *local* to refer to a particular assignment of values for a random variable, as opposed ⁹⁷ to *global* which applies to all values. Formally, for an *event of interest* Y and its potential causes 98 $X = (X^1, \ldots, X^N)$, given the value of $X = x$, local dependencies focus on which X^i s are the 99 state-specific cause of the outcome event $Y = y$ (for simplicity of presentation, in this section we 100 overload N as the number of potential causes rather than number of variables and p as the transition ¹⁰¹ function according to a subset of the variables). Formally, we denote the general data generation 102 process of Y as $p : X \to Y$ and the data generation process when Y is *only influenced* by a subset of 103 \overline{X} as $p^{\overline{X}}$: $\overline{X} \to Y$, where $\overline{X} \subseteq X$. Then, given the value of all variables, $X^1 = x^1, \dots, X^N = x^N$ and $Y = y$, we say Y locally depends on \overline{X} , if \overline{X} is the *minimal* subset of X such that knowing their 105 values is necessary and sufficient to generate the result of $Y = y$, i.e.,

$$
\underset{\bar{X} \subseteq X}{\arg \min} |\bar{X}| \qquad \text{s.t.} \quad p^{\bar{X}}(Y = y | \bar{X} = \bar{x}) = p(Y = y | X = x), \tag{1}
$$

where $|\bar{X}|$ is the number of variables in \bar{X} . For example, suppose that a robot opens a refrigerator door in a particular transition. The event of interest Y is the refrigerator door becoming open, and it locally depends on two factors: the robot and the refrigerator door, while other state factors such as objects inside the refrigerator do not locally influence Y .

110 To identify local dependencies, one can conduct a conditional independence test $y \perp x^{i} \left\{ x/x^{i} \right\}$ to 111 examine whether a variable X^i is necessary for predicting $Y = y$. In prior works, one form of this ¹¹² test is to examine whether the pointwise conditional mutual information (pCMI) is greater than 0,

$$
pCMI(y; x^{i} | \{x/x^{i}\}) = \log \frac{p(y|x)}{p^{\{X/X^{i}\}}(y | \{x/x^{i}\})} > 0.
$$
 (2)

113 If so, then it suggests that knowing $X^i = x$ provides additional information about Y that is not 114 present in $\{X/\overline{X}^i\}$, and Y locally depends on X^i . As the data generation processes are generally ¹¹⁵ unknown, one has to approximate them with learned models. Recent work in RL has utilized various ¹¹⁶ approximations such as attention weights [\[51\]](#page-12-4), Granger causality [\[13\]](#page-10-5), and input gradients [\[60\]](#page-13-1).

117 In this work, for a transition $(S = s, A = a, S' = s')$, the event of interest is each next state factor ¹¹⁸ being $(S^i)' = (s^i)'$, and we infer whether it locally depends on each state factor S^j and the action A 119 (i.e., whether there is an interaction between state factors i and j, where factor j influences i). Then ¹²⁰ we aggregate all local dependencies into a state-specific dependency graph (abbreviated in this work to 121 *dependency graph*). This overall dependency graph is represented with $\mathbb{G}(s, a, s') = \{0, 1\}^{N \times (N+1)}$,

Figure 2: During **skill learning** of SkiLD, the graph-selection policy specifies desired local dependencies for the skill policy to induce, and the induced dependency graph is identified by the dynamics model and used to update both policies. During task learning (right), the skill policy is kept frozen and a task policy is trained to select skills to maximize task reward.

122 and an edge $\mathbb{G}^{ij}(s, a, s')$ denotes, during the transition (s, a, s') , that state factor $(s^i)'$ (the "Y = y") 123 locally depends on s^j (one of the X^j):

$$
\mathbb{G}^{ij} := \text{pCMI}((x^i)'; x^j | \{x/x^j\})\tag{3}
$$

¹²⁴ This graph is used to enhance skill representation, as explained in detail in Section [3.](#page-3-1)

¹²⁵ 3 Skill Discovery from Local Dependencies (SkiLD)

 In this section, we describe SkiLD, which enhances the expressivity of skills using local dependencies. SkiLD represents local dependencies as *state-specific dependency graphs*, defined in Sec. [2.2.](#page-2-0) Unlike 128 previous unsupervised skill discovery methods that randomly sample the skill vector z from fixed distributions during skill learning, SkiLD requires a procedure to intelligently generate target depen- dency graphs during training. As such, SkiLD frames unsupervised skill discovery as a hierarchical RL problem, where a graph-conditioned skill policy learns to induce different local dependencies using primitive actions, and a high-level graph selection policy chooses which local dependencies the skill policy should induce next to guide exploration and skill-policy learning.

134 This requires formalizing two components: (1) the skill representation Z for the skill policy 135 $\pi_{\text{skill}}(a|s, z)$ and its corresponding reward function $\mathcal{R}_{\text{skill}}$, presented in Sec. [3.1,](#page-3-2) and (2) the graph 136 selection policy $\pi_{\mathbb{G}}(z|s)$ and its reward function $\mathcal{R}_{\mathbb{G}}$, presented in Sec. [3.2.](#page-4-0)

¹³⁷ 3.1 Skill Policy

 Prior unsupervised skill discovery methods usually focus skill learning on changing the state or each factor diversely. Consequently, they are can be limited to learning simple skills, for example, only changing the easiest-to-control factor in the state (i.e., the agent itself). To address this problem, SkiLD not only focuses on changing the state but also considers the interactions between state factors.

¹⁴² Skill Representation. SkiLD represents the skill space as the combination of two components: 143 $\mathcal{Z} = \mathbb{G} \times \mathcal{B}$, where $g \in \mathcal{G}$ is a state-specific dependency graph that specifies the *desired* local 144 dependencies between state factors, and $b \in \mathcal{B}$ is a diversity variable the same as that used in 145 Eysenbach et al. [\[18\]](#page-10-2). Together $z \in \mathcal{Z}$ guides the agent to change the state distinguishably while 146 inducing particular local dependencies. Specifically, the dependency graph is represented as a ¹⁴⁷ binary matrix $\mathbb{G} = \{0,1\}^{N \times (N+1)}$, where each edge \mathbb{G}^{ij} denotes, during the transition (s, a, s') , 148 whether the state factor $(s^i)'$ locally depends on s^j . The diversity variable \tilde{B} can be either discrete or 149 continuous. In this work, without loss of generality, we use a discrete space of $\{1, \ldots, K\}$ where K 150 is a predefined number. During skill training, we sample the diversity variable b from a fixed uniform 151 distribution $p(b)$, following the procedure of Eysenbach et al. [\[18\]](#page-10-2).

Given this skill space, SkiLD learns skills as a skill-conditioned policy $\pi_{\text{skill}} : S \times \mathcal{Z} \rightarrow \mathcal{A}$, where π_{skill} is trained to reach diverse states while ensuring that the local dependencies specified by the ¹⁵⁴ graph are induced. During skill learning, we select actions by iteratively calling the skill policy π_{skill} , and we denote g_{induced} as the graph that describes the local dependencies induced in a transition 156 (s, a, s') when executing a selected action a. We design the reward function of SkiLD as:

$$
\mathcal{R}_{\text{skill}} = \mathbb{1}[g_{\text{induced}} = g] \cdot (1 + \lambda \mathcal{R}_{\text{diversity}}), \tag{4}
$$

157 where $\mathbb{1}[g_{induced} = g]$ measures whether the induced dependency graph matches the desired graph, $R_{\text{diversity}}$ is the weighted diversity reward that further encourages visiting diverse states when the 159 desired graph is induced, and λ is the coefficient of diversity reward. In the following paragraphs, we 160 describe how we infer $g_{induced}$ and estimate $\mathcal{R}_{diversity}$ for each transition.

161 Inferring Induced Graphs. To infer the induced graph for a transition $(S = s, A = a, S' = s')$, 162 we need to determine, for each $(S')^i$, whether it locally depends on each factor S^j and the action 163 A. Specifically, following Sec. [2.2,](#page-2-0) we evaluate the conditional dependency $(s^i)' \not\perp s^j | \{s/s^j, a\}$ ¹⁶⁴ by examining whether their pointwise conditional mutual information (pCMI) is greater than a predefined threshold $pCMI^{ij} = \frac{p((s^i)'/|s,a)}{p((s^i)'/|s/s')/|s'|}$ 165 predefined threshold pCMI^{ij} = $\frac{p((s^t)'|s,a)}{p((s^i)'|\{s/s^j,a\})} \ge \epsilon$. If so, it suggests that s^j is necessary to predict 166 $(s^i)'$ and thus the local dependency exists. Meanwhile, as the transition probability p is unknown, we ¹⁶⁷ approximate it with a learned dynamics model that is trained to minimize prediction error. 168 Finally, after obtaining the induced dependency graph, we evaluate $\mathbb{1}[g_{induced} = g]$ by examining 169 whether each edge $g_{induced}^{ij}$ matches the corresponding edge in the desired graph g^{ij} . As \mathcal{R}_{skill} only

¹⁷⁰ provides sparse rewards to the skill policy when the desired graph is induced, we use hindsight ¹⁷¹ experience replay [\[1\]](#page-9-3) to enrich learning signals, by relabelling induced graphs as desired graphs in ¹⁷² some episodes.

173 Diversity Rewards. When the skill policy induces the desired graph, $\mathcal{R}_{\text{diversity}}$ further encourages ¹⁷⁴ it to visit different distinguishable states under different diversity indicators b, e.g., driving the nail ¹⁷⁵ to different locations. This diversity enhances the applicability of learned skills. To this end, we 176 design the diversity reward $\mathcal{R}_{\text{diversity}}$ as the forward mutual information between visited states and the 177 diversity indicator $I(s; b)$, following DIAYN. To estimate the mutual information, we approximate 178 it with a variational lower bound $I(s; b) \geq q(b|s)$, where $q(b|s)$ is a neural network discriminator ¹⁷⁹ trained to predict the diversity indicator b from the visited state. In practice, rather than learning a ¹⁸⁰ single low-level skill to handle all graphs and diversity parameters, we utilize a factorized lower-level ¹⁸¹ policy, where there is a separate policy for each factor. More details about this subdivision can be ¹⁸² found in Appendix [A.](#page-14-0)

¹⁸³ 3.2 Graph-Selection Policy

184 To acquire skills that are useful for downstream tasks, π_{skill} needs to learn to induce a wide range of local dependencies *sample-efficiently*. To this end, we propose to learn a graph-selection policy $\pi_{\mathbb{G}} : S \to \mathbb{G}$ to guide the training of π_{skill} . Specifically, training π_{skill} requires a wise selection of 187 graphs — as graph space $\mathbb G$ increases super-exponentially in the number of state factors N, many graphs are not inducible. To this end, we only select target graphs for skill policy from a history of all seen graphs. As the agent learns to induce existing graphs in diverse ways, new graphs may be encountered, gradually expanding the set of seen graphs.

 However, though this history guarantees graph inducibility, two challenges still remain: (1) How to efficiently explore novel local dependencies, especially hard-to-visit ones? (2) For all seen graphs, the use should π_{skill} learn next to maximize training efficiency? We address these challenges 194 based on the following heuristic — compared to well-learned skills, π_{skill} should focus its training on underdeveloped skills. Meanwhile, learning new skills opens up the possibility of visiting novel local dependencies, e.g., learning to grasp the hammer makes it possible for the robot to hammer the nail.

197 According to this heuristic, we learn a graph-selection policy $\pi_{\mathbb{G}}$ that guides the exploration and training of the skill policy π_{skill} . Specifically, $\pi_{\mathbb{G}} : \mathcal{S} \to \mathbb{G}$ selects a new dependency graph the skill 199 policy should induce for the next L time steps. To increase the likelihood of visiting hard graphs, $\pi_{\mathbb{G}}$ ²⁰⁰ is trained to maximize the following graph novelty reward

$$
\mathcal{R}_{\mathbb{G}} = \frac{1}{\sqrt{C(g_{\text{visited}})}},\tag{5}
$$

201 where $C(g_{\text{visited}})$ is the number of times that we have seen the graph in the collected transition. While ²⁰² Eq. [5](#page-4-1) is similar to state-count-based exploration reward, here, it is based on the count of dependency ²⁰³ graphs, and thus applicable to both discrete and continuous state space.

Figure 3: Evaluation domains: Mini-behavior: Installing Printer, Thawing and Cleaning Car, and iGibson.

3.3 Downstream Task Learning

 In SkiLD, we utilize hierarchical RL to solve reward-supervised downstream tasks with the discovered 206 skills. The skill policy, π_{skill} acts as the low-level policy while a task policy, $\pi_{\text{task}} : S \to Z$, is learned 207 to select which skill $z = (q, b)$ to execute for L steps. Compared to diversity-based skills that are limited to simple behaviors, our local-dependency-based skills enable a wide range of interactions between state factors, leading to more efficient exploration and superior performance of downstream tasks learning.

4 Experiments

212 In this section we aim to provide empirical evidence towards the following questions: \mathbf{Q} 1) Do 213 the skills learned by SkiLD induce a diverse set of interactions among state factors? $Q2$) Do the skills learned by SkiLD enable more efficient downstream task learning compared to other [u](https://sites.google.com/view/skild/)nsupervised reinforcement learning methods? Our learned skills can be visualized at [https:](https://sites.google.com/view/skild/) [//sites.google.com/view/skild/](https://sites.google.com/view/skild/).

4.1 Domains

 In this work, we focus on addressing the challenge of vast state space brought by a large number of state factors. Hence, we evaluate our method on two challenging *object-rich* embodied AI benchmarks: Mini-behavior [\[30\]](#page-11-2) and Interactive Gibson [\[40\]](#page-11-3).

221 The Mini-behavior (Mini-BH) domain [\[30\]](#page-11-2) (Figure [3a](#page-5-0)) contains a set of gridworld environments where an agent can move around and interact with a variety of objects to accomplish certain household tasks. While conceptually simple, this domain has been shown to be extremely challenging for Vanilla RL with sparse reward [\[30\]](#page-11-2). Each Mini-BH environment contains different objects and different success criteria. We tested on three particular environments in Mini-behavior, including:

- Installing Printer: A relatively simple environment with three state factors: the agent, a table, and a printer that can be installed.
- **Cleaning Car**: An environment where the objects have rich and complex interactions. The state factors include the agent, a toggleable sink, a piece of rag that can be soaked in the sink, a car that the rag can clean, a soap and a bucket which can together be used to clean the rag.
- **Thawing:** An environment with lots of movable objects. The state factors include the agent, a sink, a fridge that can be opened, and three objects that can be thawed in the sink: fish, olive, and a date.

 The Interactive Gibson (iGibson) domain [\[41\]](#page-11-4) (Figure [3b](#page-5-0)) contains a realistic simulated Fetch Robot that operates in a kitchen environment with a refrigerator, sink, knife, and peach. The peach can be washed or cut. This domain is very difficult especially when using low-level motor commands because much of the domain is free space, meaning that only a minute fraction of action sequences will manipulate the objects meaningfully.

 Both Mini-BH and iGibson require learning long-horizon policies spanning many low-level actions from sparse reward, making these challenging domains (see details in Appendix).

²⁴⁰ 4.2 Baselines

²⁴¹ Before evaluating the empirical questions, we provide a brief description of the baselines. These ²⁴² baselines include unsupervised skill learning, and causal and hierarchical methods.

243 Diversity is all you need (DIAYN [\[18\]](#page-10-2)): This method learns unsupervised state-covering skills using a mutual information objective. SkiLD utilizes a version of this for state-diversity skills modulated by a desired dependency graph. This baseline determines how incorporating graph information affects the algorithm.

²⁴⁷ Controllability-Aware Skill Discovery (CSD [\[48\]](#page-12-1)): Extends DIAYN with a factorization based on ²⁴⁸ controllability. This baseline is a comparable skill learning method that leverages state factorization ²⁴⁹ but does not encode local dependencies.

²⁵⁰ Exploration via Local Dependencies (ELDEN [\[60\]](#page-13-1)): This method utilizes gradient-based techniques ²⁵¹ to infer local dependencies for exploration. However, without a skill learning component, it can ²⁵² struggle to chain together complex behavior.

253 Chain of Interaction Skills (COInS [\[13\]](#page-10-5)): This is a hierarchical algorithm that constructs a chain ²⁵⁴ of skills using Granger-causality to identify local dependencies. Because it is restricted to pairwise ²⁵⁵ interactions, it struggles to represent the rich policies necessary for these tasks.

²⁵⁶ Vanilla RL: This baseline uses PPO [\[55\]](#page-12-5) to directly train an agent with the extrinsic reward. Unlike ²⁵⁷ other baselines, this method does not have a pertaining phase. Since all the task rewards are sparse ²⁵⁸ and the tasks are often long horizon, vanilla RL often struggles.

²⁵⁹ 4.3 Interaction Graph Diversity

 We first evaluate whether SkiLD is indeed ca- pable of achieving complex interaction graphs (Q1), comparing against two strong skill discov- ery baselines introduced earlier: DIAYN and ²⁶⁴ CSD.

 Each of these methods is trained for 10 Million steps without having access to any reward. Then to evaluate their learned skills, we unroll each of them for 500 episodes with randomly sam- pled skills z and examine the diversity of the interaction graphs they can induce. Figure [4](#page-6-0) illustrates the percentages of episodes where particular local dependencies have been induced at least once, in Mini-BH Cleaning Car. We find that DIAYN and CSD are limited to skills that only manipulate one object individually, i.e. 276 (agent, rag, action \rightarrow rag) or (agent, soap, action $277 \rightarrow$ soap). By contrast, SkiLD learns to induce more complicated causal interactions, such as 279 soaking the rag in the sink (sink, rag \rightarrow rag) and cleaning the car with the soaked mug (car, rag $281 \rightarrow \text{car}$).

Figure 4: The percentage of episodes where a dependency graph is induced through random skill sampling. Standard deviation is calculated across five random seeds.

²⁸² 4.4 Performance

²⁸³ Next, we evaluate whether the local dependency coverage provided by SkiLD leads to a performance ²⁸⁴ boost in downstream task learning (Q2). We follow the evaluation setup in the unsupervised rein-²⁸⁵ forcement learning benchmark [\[36\]](#page-11-5), where for a given environment, an agent is first pre-trained 286 without access to task reward for K_{pt} steps, and then finetuned for K_{ft} steps. Importantly, the same ²⁸⁷ pre-trained skills are reused on multiple distinct downstream tasks within the same environment, so 288 that only the upper-level skill-selection policy is task-specific. We have $K_{pt} = 2M$, $K_{ft} = 1M$ for 289 installing printer, $K_{pt} = 10M$, $K_{ft} = 5\overline{M}$ for thawing and cleaning car, and $K_{pt} = 4M$, $K_{ft} = 2M$

Figure 5: Training curves of SkiLD and baselines on multiple downstream tasks (reward supervised second phase). Each curve depicts the mean and standard deviation of the success rate over 5 random seeds. SkiLD outperforms all baselines for most tasks, converging faster and to higher returns.

²⁹⁰ for iGibson, and evaluate each method for each task across 5 random seeds. Hyperparameter details ²⁹¹ can be found in Appendix [D.](#page-16-0) Specifically, we evaluate on the following downstream tasks:

²⁹² • Installing Printer: We have a single downstream task in this environment, where the agent needs ²⁹³ to pick up the printer, put it on the table, and turn it on.

²⁹⁴ • **Thawing**: We have three downstream tasks: thawing the fish or the olive or the date.

²⁹⁵ • Cleaning Car: We consider three downstream tasks, where each task is a pre-requisite of the ²⁹⁶ following one. The tasks are: soak the rag in the sink; clean the car with the rag; and clean the dirty ²⁹⁷ rag using the soap in the bucket.

298 • IGibson: The tasks for this domain are: grasping the peach, washing the peach in the sink, and ²⁹⁹ cutting the peach with a knife.

300 After skill learning, we train a new upper-level policy that uses z as actions and is trained with extrinsic reward, as described in Section [3.3.](#page-5-1) Figure [5](#page-7-0) illustrates the improvement of SkiLD as compared to other methods. Without combining dependency graphs with skill learning, other methods struggle with any but the simpler tasks. COInS performs poorly because of its chain structure, which restricts the agent controlling policy from picking up objects. ELDEN's exploration reaches graphs, but without skills struggles to utilize that information in downstream tasks. DIAYN learns skills, but few manipulate the objects, so a downstream model struggles to utilize those skills to achieve meaningful rewards. By comparison, SkiLD achieves superior performance on 9 of the 10 downstream tasks evaluated. In the two hardest tasks which require a very long sequence of precise controls, Clean Rag and Cut Peach, SkiLD is the only method that can achieve a non-zero success rate (although still far from fully mastering the tasks), showcasing the potential of local dependencies for skill learning.

311 4.5 Graph and Diversity Ablations

 We also explore the functionality of the graph and diversity components of the skill parameter z by assessing the downstream performance of SkiLD without these components. This produces two ablative versions of SkiLD: SkiLD without diversity and SkiLD without dependency graphs. To isolate learning from the effect of learned local dependencies, we use ground truth dependency graphs for ablative evaluations where relevant. In Figure [6,](#page-8-0) learning without graphs results in zero performance, consistent with DIAYN results. In addition, removing diversity produces a notable decline in performance, especially on more challenging tasks like clearning the rag. These evaluations demonstrate that SkiLD benefits from both the incorporation of dependency graphs and diversity.

Figure 6: A figure illustrating the ablative performance of SkiLD without diversity or without graphs. Without graphs, the method collapses completely, while removing diversity results in a noticeable reduction in downstream performance.

5 Related Work

 This work lies in the unsupervised skill learning framework [\[35\]](#page-11-6), where the agent must discover a set of useful skills which are reward independent. It then extends these skills to construct a 2-layer hierarchical structure [\[58\]](#page-12-6), where the upper policy receives reward both for achieving novel skills, and can then be tuned to utilize the learned skills to accomplish an end task. Finally, the skills are identified using token causality, a specific problem identified in causal literature.

5.1 Unsupervised Skill Learning

 This work describes a framework for utilizing local dependency graphs and diversity to discover unsupervised skills. Diversity-based state coverage skills have been explored in literature [\[18\]](#page-10-2) 329 utilizing forward and backward mutual information techniques to learn a goal space \mathcal{Z} , and a skill 330 encoder $q(z|\cdot)$ [\[10\]](#page-9-4). This unsupervised paradigm has been extended with Lipschitz constraints [\[47\]](#page-12-7), contrastive objectives [\[37\]](#page-11-7), information bottleneck [\[33\]](#page-11-8), population based methods such as particle estimation [\[43\]](#page-12-8), quality diversity [\[42\]](#page-12-9) and mixture of experts [\[11\]](#page-10-6). These skills can then be used for hierarchical policies or planners [\[54,](#page-12-10) [64,](#page-13-2) [22\]](#page-10-7), which mirrors the same structure as SkiLD. Unlike these methods, SkiLD adds additional subdivision through dependency graphs, which mitigates the combinatorial explosion of skills that can result from trying to cover a large factored space.

5.2 Hierarchical Reinforcement Learning

 The hierarchical policy structure in SkiLD where a higher level policy passes a parameter to be inter- preted by low-level planners has been formalized in [\[58\]](#page-12-6), and learned using deep networks utilizing extrinsic reward [\[2,](#page-9-5) [59\]](#page-12-11), attention mechanisms [\[15\]](#page-10-8), initiation critera [\[32,](#page-11-9) [3\]](#page-9-6) and deliberation cost [\[25\]](#page-10-9). Hierarchies of goal-based policies [\[38\]](#page-11-10) has been extended with object-centric representations [\[63\]](#page-13-3), offline data [\[46\]](#page-12-12), empowerment [\[39\]](#page-11-11) and goal counts [\[49\]](#page-12-13). In practice, SkiLD uses graph and diversity parameters similar to goal-based methods. However, the space of goals can often be intractable large, and methods to address this use graph laplacians [\[34\]](#page-11-12) causal chains [\[12,](#page-10-10) [13\]](#page-10-5) or general causal relationships [\[27\]](#page-10-4). SkiLD is similar to these causal methods but utilizes local dependence along with general two-layer architectures, thus showing increased generalizability.

5.3 Causality in Reinforcement Learning

 This work investigates the application of local dependency to hierarchical reinforcement learning. This kind of reasoning has been described as "local causality" or "interactions" in prior RL work for data augmentation [\[51,](#page-12-4) [52\]](#page-12-14), learning skill chains [\[12,](#page-10-10) [13\]](#page-10-5) and exploration [\[60\]](#page-13-1). This work is the first synthesis of unsupervised skill learning and local dependencies applied to general 2-layer hierarchical reinforcement learning. Other general causality work investigates action-influence detection [\[56,](#page-12-3) [26\]](#page-10-11), affordance learning [\[9\]](#page-9-7), model learning [\[28,](#page-11-13) [20\]](#page-10-12), critical state identification [\[44\]](#page-12-15), and disentanglement [\[16\]](#page-10-13). In the context of relating local dependency and causal inference, we provide a discussion in Appendix [C.](#page-15-0) SkiLD incorporates causality-inspired local dependence to skill learning, resulting in a robust set of transferable skills.

6 Conclusion

 Unsupervised skill discovery is a powerful tool for learning useful skills in long-horizon sparse reward tasks. However, many unsupervised skill-learning methods do not take advantage of factored environments, resulting in poor performance in complex environments with several objects. Skill Discovery from Local Dependencies utilizes state-specific dependency graphs, identified using learned pointwise conditional mutual information models, to guide skill discovery. The framework of defining skills according to a dependency graph and diversity goal, combined with a learned sampling scheme, achieves difficult downstream tasks. In domains where hand-coded primitive skills are typically given to the agent, like Mini-behavior and Interactive Gibson, SkiLD can achieve high performance without requiring explicit domain knowledge. These impressive results arise intuitively from incorporating local dependencies as skill targets, illuminating a meaningful direction for unsupervised skill learning to be applied to a wider array of environments.

 Limitations and Future Work An important assumption of SkiLD is its access to factored state space. While factored state space can often be naturally obtained from existing RL benchmarks and many real-world environments, developments in disentangled representation learning [\[45,](#page-12-2) [29\]](#page-11-1) will help with extending SkiLD to unfactored image domains. Secondly, SkiLD requires accurate detection of local dependencies. While off-the-shelf methods [\[60,](#page-13-1) [56\]](#page-12-3) work well for detecting local dependencies in our experiments, future works that can more accurately detect local dependencies will be beneficial to the performance of SkiLD.

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A Factored Skills

565 Learning to reach both a desired graph g and a diversity parameter b through primitive actions is challenging. First, different graphs often have substantially different characteristics, with some graphs that are easy to achieve (eg. action→agent), and others that are quite challenging and rare (eg. agent, knife, fruit→fruit). Not only would it be challenging for a single policy to encode all of these behaviors, the diversity parameter notwithstanding, but over-training the frequency at which certain graphs are called might vary significantly. Rather than trying to learn a single monolithic policy, then, 571 we instead structure the skill parameterized policy π_{skill} as a collection of factored skills: $\pi_{\text{skill},i}$, for 572 each factor $i \in \{1, \ldots, N\}$.

 This modification to the policy structure results in three changes: 1) The upper-level action space passes a single row of the graph G, denoted with g_i , and the desired factor i. 2) Instead of achieving 575 an entire graph use the achieved row $\mathbb{1}[g_{\text{achieved},i} = g_i]$. 3) The history of seen graphs H is replaced 576 with a history of factored graph rows \mathcal{H}_f .

577 Define the history of graph rows as $\mathcal{H}_f := \{\text{unique } (i, g_{\text{achieved}}, \forall i \in 1, ..., N \ \forall g_{\text{achieved}} \in \mathcal{D})\}.$ This takes the unique graph rows from all those seen in previous data. Then the upper policy uses the same historical sampling procedure as with unfactorized graphs: the policy samples discretely from the new history, which will by default return i, g_i , a graph row, and the desired factor. This resolves 581 points 1,3. Point 2 is addressed by replacing Equation [4](#page-4-2) with $\mathbb{1}[g_{\text{achieved},i} = g_i]$.

 Empirically, we found that without this change, the lower policy rarely learns anything, even simple control of the agent.

B Environment Details

 In this section, we provide a detailed description of the environment, including its semantic stages representing internal progress toward task completion, state space, and action space. We also highlight that while each task consists of multiple semantic stages, agents do not have access to this information.

Figure 7: Environments.

 Installing Printer As shown in Fig. [7\(](#page-14-1)a), the Installing Printer environment is relatively simple, consisting of 3 factors: the agent, a printer, and a table. The task requires the agent to complete the following stages: (1) pick up the printer, (2) bring the printer to and place it on the table, and (3) turn on the printer. The discrete state space consists of (i) the agent's position and direction, (ii) the positions of the printer and whether it is on or off, and (iii) the position of the table. The discrete action space consists of (i) moving forward, turning left or right, (ii) picking up / placing down the printer, and (iii) turning on / off the printer.

Thawing As shown in Fig. [7\(](#page-14-1)b) and Fig. [8\(](#page-18-0)a), the Thawing environment consists of 6 factors: the agent, a sink, a refrigerator, and three frozen objects: fish, olive, and date. Thawing each object requires the agent to complete the following stages: (1) move to and open the refrigerator, (2) take the frozen fish out of the refrigerator, (3) put the fish into the sink, and (4) turn on the sink to thaw it. The discrete state space consists of (i) the agent's position and direction, (ii) the positions of all environment entities, (iii) whether the sink door is turned on, (iv) whether the refrigerator door is opened, and (v) the thawing status of three objects. The discrete action space consists of (i) moving forward, turning left or right, (ii) opening / closing the refrigerator, (iii) turning on / off the sink, and (iv) picking up / placing down each object.

 Cleaning Car As shown in Fig. [7\(](#page-14-1)c), the Cleaning Car environment consists of 7 factors: the agent, a car, a sink, a bucket, a shelf, a rag, and a piece of soap. Cleaning both the car and the rag requires ϵ_{06} the agent to complete the following **stages**: (1) take the rag off the shelf, (2) put it in the sink, (3) toggle the sink to soak the rag up, (4) clean the car with the soaked rag, (5) take the soap off the self, and (6) clean the rag with the soap inside the bucket. The discrete state space consists of (i) the agent's position and direction, (ii) the positions of all environment entities, (iii) whether the sink is turned on, (iv) the soak status of the rag, (v) the cleanness of the rag, and (vi) the cleanness of the car. The discrete action space consists of (i) moving forward, turning left or right, (ii) turning on / off the sink, and (iii) picking up / placing down the rag / soap.

 iGibson As shown in Fig. [7\(](#page-14-1)d), the iGibson environment consists of 4 factors: the robot, a knife, a peach, and a sink. The robot can do the following things: (1) grasp peach: move close to the peach and grasp it, (3) wash peach: grasp the peach and place it into the sink, (3) grasp knife: move close to the knife and grasp it, (4) cut peach: grasp the knife and use it to cut the peach. The continuous state space consists of (i) the robot's proprioception, (ii) the poses of all environment entities, and (iii) whether the peach is cut. The continuous action space consists of (i) end-effector position change, (ii) base linear and angular velocity, and (iii) gripper torque (to open/close the gripper).

620 C Local Dependencies and Causal Inference

 \mathfrak{so}_{21} In this work, we define local dependencies according to the state factors $X = (X^1, \ldots, X^N)$ 622 and event of interest Y, which in the context of an MDP is a subset of the next state factors 623 $X' = (X^{1}, \ldots, X^{N})$. In the factored MDP formulation [\[7\]](#page-9-1), we assume that p, the transition ⁶²⁴ dynamics, are represented by a dynamic Bayesian network (DBN) which is a time-directed bipartite ezs graph, with edges only from factors in X to factors in X' . In this work, we assume that the underlying 626 ground truth DBN, that is the transition function p , can be decomposed according to subsets of state 627 factors \bar{X} , such there exists a $p^{\bar{X}}(Y=y|\bar{X}=x)$ for every state.

⁶²⁸ The factored transition dynamics analogizes with causal inference in the following way: If the state ⁶²⁹ factors and next state factors are each assigned a causal variable by adding the assumption that they ⁶³⁰ can be independently intervened on, and each next state variable carries an associated unobserved 631 noise variable U^i , which we assume is independent of any X^k not connected to $X^{'j}$ and any other 632 next state variable $X^{i,j}$, then we can represent the transition dynamics p with a structural causal model 633 (SCM) [\[50\]](#page-12-16), a graph connecting the causal variables in X to the causal variables in X' .

 634 For a particular outcome variable Y that is one of the next state causal variables X' , we can describe ⁶³⁵ local dependence in the RL context according to assumptions about the structural causal model. 636 Represent the non-noise parents of Y as pa(Y), and the noise parents as $pa_U(Y)$. Under normal 637 causal assumptions, the structural causal model for Y is a function $f_Y(\text{pa}(Y), \text{pa}_U(Y)) = Y$. Define \bar{X} as a subset of the endogenous parents of Y and \bar{U} as an equivalent subset of the noise variables. Further define the values that $pa(Y)$, $pa_U(Y)$, \overline{X} , \overline{U} can take on as $pa(y)$, $pa_U(y)$, \overline{x} , \overline{u} respectively, 640 and $(pa(y), \mathcal{X}, \mathcal{U}$ as the set of states the parents of Y, the variables in X and variables in U can take ⁶⁴¹ on respectively.

 642 To formalize local invariance, we add the assumption that f_Y can be decomposed into a series of func-643 tions $(f_{Y1}(\bar{X}_1 = \bar{x}_1, \bar{U}_1 = \bar{u}_1), \dots, f_{Yk}(\bar{X}_k = \bar{x}, \bar{U}_k = \bar{u}_k)$ and $g_Y(\text{pa}(Y) = \text{pa}(y), \text{pa}_U(Y) = \bar{u}_1$ $p_{\mathbf{a}_{I}}(y)$, where each $f_{Y_i}: \overline{\mathcal{X}} \times \overline{\mathcal{U}} \to \mathcal{Y}$ and $g : pa(\mathcal{Y}) \to \{1, \ldots, k\}$, a function mapping the parents 645 of Y to one of the functions. Then if f is represented as:

$$
f(pa(x), pa_U(y)) := \sum_{i=1}^{k} \mathbb{1}(g_Y(pa(y), pa_U(y)) = i) f_{Yi}(\bar{x}_i, \bar{u}_i)
$$
(6)

646 The local dependence of $Y = y$ in a particular state (x, x') is then the set of variables in \overline{X}_i for the 647 particular i where $\mathbb{1}(q_Y(\text{pa}(y), \text{pa}_U(y))) = i) = 1$, and the pCMI test is a way of uncovering these ⁶⁴⁸ local dependencies from observational data.

 Local dependence has been investigated in the field of context-specific independence [\[53,](#page-12-17) [8\]](#page-9-8), which seeks to find particular assignments of a subset of the causal variables under which an outcome is independent of some subset of the inputs. In particular, context-set specific independence [\[8\]](#page-9-8) determines if a variable is independent of other variables on a particular subset of states, described as

Table 1: Parameters of Skill Learning and Task Learning. Parameters shared if not specified.

⁶⁵³ the partial context set. While our work uses the pCMI test described in Equation [3,](#page-3-3) context-specific ⁶⁵⁴ independence focuses on complete independence using knowledge of the structural model.

655 Alternatively, interactions can be viewed as the causes (X) of particular effects (Y) , which have also been investigated under the description of token or actual cause [\[24\]](#page-10-14) (as opposed to general cause). Actual cause utilizes a series of counterfactual tests to determine if a cause is necessary, sufficient, and minimal for an outcome. Actual cause has primarily been applied in simple, discrete examples [\[4,](#page-9-9) [23\]](#page-10-15), making it difficult to directly apply to RL. However, recent work has incorporated the notion of context-specific independence and extended actual cause to more complex domains [\[14\]](#page-10-16).

⁶⁶¹ D Implementation Details

 The hyperparameters of skill learning and task learning can be found in Table [1.](#page-16-1) As it is challenging to identify local dependencies using learned dynamics models in Thawing and iGibson environments, we use ground truth local dependencies from simulator. The codebase is built on tianshou [\[61\]](#page-13-4) for backend RL, though with significant modifications.

⁶⁶⁶ The 5 seeds selected are 0 - 4. The experiments were conducted on machines of the following ⁶⁶⁷ configurations:

- ⁶⁶⁸ Nvidia A40 GPU; Intel(R) Xeon(R) Gold 6342 CPU @2.80GHz
- ⁶⁶⁹ Nvidia A100 GPU; Intel(R) Xeon(R) Gold 6342 CPU @2.80GHz

₆₇₀ E Skill Visualizations

In Figure [8](#page-18-0) we visualize three challenging long-horizon skills learned by SkiLD: thawing the olive,

cleaning the car, and cutting the peach. All of these skills require a sequence of interactions that

is difficult to recover without directed behavior. Thus, comparable baselines do not learn skills of

similar complexity. More skill visualizations can be found at: [https://sites.google.com/view/skild.](https://sites.google.com/view/skild)

Figure 8: Policy rollouts for learned policies that achieve long horizon tasks (a) Mini-BH thaw olive, (b) Mini-BH clean car, (b) iGibson cut peach.